

Implementation of Baugh-Wooley Multiplier and Modified Baugh Wooley Multiplier Using Cadence (Encounter) RTL

Pramod S. Aswale, Mukesh P. Mahajan, Manjul V. Nikumbh, Omkar S. Vaidya

Abstract— High speed, low power consumption are key requirement to any VLSI design. The power efficient multipliers play an important role. This paper presents an efficient implementation of a high speed, low power multiplier using shift and adds methods of Baugh Wooley Multiplier. This study presented the design and implementation of Baugh wooley multipliers using Cadence (Encounter) RTL Compiler. In this work, Modified Baugh Wooley is having least area, power and delay. The Modified Baugh wooley architecture is 109X faster than Conventional array multiplier and 102X faster than conventional Baugh Wooley. The operating frequency of 5 x 5 Design Modified Baugh Wooley multiplier is 160MHz. The Selection of Multiplier should be done depending on performance measure and application nature.

Index Terms— Baugh Wooley, Cadence, Low Power Multiplier, RTL Compiler.

I. INTRODUCTION

The increasing prominence of portable system and the need to limit power consumption in very high density ULSI chips have led to rapid and innovative developments in low power design. The need for low power design is becoming a major issue in high performance digital systems, such as micro-processor, digital signal processing and other applications. As demands for portable computing and communication are growing, the power efficient multiplier plays an important role in Very Large Scale Integration (VLSI) system design. Multiplication is one of the essential operation in many algorithm used in Digital Signal Processing (DSP). A primary requirement of high performance digital system is high speed multiplication. In many cases multiplier may be present in critical path and speed of processing is ultimately get reduced by speed of multiplication. The Multiplier algorithm is also one of the major contributors to the total power dissipation. Reducing the power dissipation is key criteria in design of multiplier. Power consumed by multipliers can be lowered at various levels of the design from algorithm to architectures to circuit [15]. The core of

any processor is the arithmetic and logic unit (ALU). The ALU combines the addition and subtraction with other operation. The addition and subtraction of two numbers are the basic operation in all digital computers. These operations occur at the machine instruction level and are implemented using the basic logic gates in arithmetic and logic unit (ALU) subsystem of the microprocessor. The time needed to perform these operations affects the performance of processors. Multiplication is one of the important operations which requires more complex circuitry than addition/subtraction operations. Multiplications are expensive and slow operations. In many computational problems the performance is dominated by the speed at which a multiplication operation can be executed.

Multipliers are complex adder arrays. Multiplication consists of three basic operations: the generation of partial product, reduction of partial products, final carry propagate summation [21]. Considering the timing constraints, dedicated multipliers hardware implementations such as array multiplier were introduced. Variable size partial product arrays are not practical for multiplier design and since a more sophisticated methods were proposed. The modified booth recoding scheme is one of the more popular implementation. The advantage of modified booth recoding algorithm is that, it reduces the number of generated partial products by half. Bit pair recoding of the multiplier derived from booth algorithm, reduces the number of summands by a factor 2. These summands can then be reduced to only two by using a relatively small number of carry save addition steps. The final product can be generated by an addition operation that uses a carry look ahead adder [19]. The partial sum adders can be rearranged in a tree like fashion, reducing both the critical path and the number of adder cells required e.g wallace tree multiplier, Dadda. Due to irregular structure, it is difficult to place and route during the layout of a multiplier. A decreased size of the reduction circuit eases the implementation and improves the performance of the multiplier [12].

There are a number of techniques that can be used to perform multiplication. The choice is based upon factors such as latency, throughput, area and design complexity. More efficient parallel approach uses some sort of array or tree of full adders to sum the partial products. The number of partial products to sum can be reduced using Booth Encoding and the number of logic levels required to perform the summation can be reduced with Wallace trees. Wallace trees are complex to layout and have long irregular wires, so hybrid structures may be more attractive. Multiplications are expensive and slow operation. Basically multiplication process may be viewed to consist of following two steps (1) Evaluation of partial product (2) Accumulation of the shifted partial product. Therefore, faster way to implement

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multiplication is to resort to an approach similar to manually computing a multiplication. All the partial products are generated at same time and organized in an array. A less number of partial products also reduces the complexity and as a result increases the speed to accumulate the partial products. Both solutions can be applied simultaneous.

In [1], full custom flow of Wallace-Tree, Array and Baugh Wooley multiplier is implemented using low power design techniques. In design the parallel multipliers, the number of partial products to be added is the key parameter which determines the performance of multiplier.

In [2] comparative study of Modified Booth Multiplication and Baugh Wooley Multiplier is carried out. The 32 bit multiplier using 65nm and 130nm is designed and simulated using Cadence software. According to [11] for a 32 bit multiplier, a Modified Booth implementation has larger power dissipation, area and only small improvement in delay compared to Baugh Wooley multiplier implementation.

The [3] presents an efficient high speed multiplier Baugh Wooley multiplier. In [3], the study of 4 bit pipelined multiplier is presented and implemented in VHDL. The parallel multiplier uses less number of adders, as result of less space is occupied compared to serial multiplier. The main criteria in the chip fabrication and high performance system requires that component should be as small as possible. Baugh wooley two's compliment signed multipliers is the best known algorithm for signed multiplication because it maximizes the regularity of the multiplier and allow all the partial products to have positive sign bits. Baugh Wooley technique was developed to design direct multiplies for twos compliment numbers. A Baugh Wooley multiplier was used for twos compliment multiplication due to its efficiency in handling signed bits. The principle advantage is that sign of all the partial products bits are positive allowing the product to be formed using array addition techniques. In conventional twos complement multiplication there are partial product bits with negative as well as positive signs.

The [4] presents the implementation of power efficient BaughWooley multiplier using FPGA Spartan 3 device. The speed, power and area have a significant impact as per the specific applications and efficient realization of the multiplication is important. The Spartan 3 AN FPGA device could be used to build basic block reasonably. Many DSP algorithm demands using application specific integrated circuits. The computation time can be speedup by assigning computation intensive tasks to hardware and by exploiting the parallelism in algorithms.

In [5], 16 X 16 bit multiplier is design and implemented. When the numbers are in the 2's complement form, the design of iterative arrays becomes difficult since the sign bit is embedded in the number itself. The two scheme which reduces these problems are the Pezaris and Baugh Wooley algorithm. The Pezaris, uses different types of cells while Baugh Wooley algorithm requires true and complemented form of both numbers.

The power consumed by multipliers can be reduced at various levels of the design from algorithms to architectures to circuit and device level. Reference [8]- [12] provides a good inside into the problem and design optimizations at all the hierarchy levels.

II. BAUGH WOOLEY TWO'S COMPLEMENT SIGNED MULTIPLIER

When the operands are in two's complement form, the design of iterative arrays becomes more difficult since the sign bit is embedded in the number itself. Direct two's complement multiplication arrays have been proposed where the cells used are either more complex or the number of cells is significantly larger than for the positive-number multiplier array [16]. Baugh and Wooley modified the multiplication matrix into a form that contains only positively weighted partial products. To accomplish this, both the true and complement values of the operands are needed. There is also a slight increase in the number of adding cells and in the multiplication time. The resulting array, however, uses only Type 0 full adder cells. This uniformity is particularly advantageous for LSI implementation. Multiplying two 2's complement numbers. Let us consider two n-bit numbers A and B can be represented as



Where the a_i 's and b_i 's are the bits in A and B respectively and a_{n-1} and b_{n-1} are sign bits. The product $P=A \times B$ is then given by the following equation.

$$\begin{aligned}
 P &= A * B = (a_{n-1}2^{n-1} + \sum_{i=0}^{n-2} a_i 2^i) * (-b_{n-1}2^{n-1} + \sum_{i=0}^{n-2} b_i 2^i) \\
 &= a_{n-1} b_{n-1} 2^{2n-2} + \sum_{i=0}^{n-2} \sum_{j=0}^{n-2} a_i b_j 2^{i+j} \\
 &= -2^{n-1} \sum_{i=0}^{n-2} a_i 2^i - 2^{n-1} \sum_{j=0}^{n-2} a_j b_j \dots \dots \dots 3 \dots
 \end{aligned}$$

Above equation indicates that the find product is obtained by subtracting the last two positive terms from the first two terms. One important complication in the development of the efficient multiplier implementation is the multiplication of two's compliment signed numbers.

Baugh Wooley two's compliment signed multipliers is the best known algorithm for signed multiplication because it maximizes the regularity of the multiplier and allow all the partial products to have positive sign bits Baugh and Wooley have proposed an algorithm for direct two's complement array multiplication. The principal advantage of their algorithm is that the signs of all summands are positive, thus allowing the array to be constructed entirely with conventional type 0 full adders, whereas Pazaris two's complement multiplier uses mixture types of full adders.

The Baugh Wooley algorithm is a relatively straightforward way of doing signed multiplications when multiplying two's complement number directly each of the partial products to be added is a signed numbers. Thus each partial product has to be sign extended to the width of the final product in order to form a correct sum by Carry Save Adder(CSA) tree.

According to Baugh Wooley approach, an efficient method of adding extra entries to the bit matrix is suggested to avoid having to deal with the negatively weighted bits in partial product matrix. In equation (write equation no here), rather than doing a subtraction operation, we can obtain the 2's complement of the last two term and add all terms to get the

final product. The last two terms are n-1 bits each that extend in binary weight from position 2^{n-1} up to 2^{2n-3} . On the other hand, the final product is 2n bits and extends in binary weight from 2^0 upto 2^{2n-1} . We pad each of the last two terms in equation 4 with zero's to obtain a 2n-bit number to be able to add them to the other terms. The padded terms extend in binary weight from 2^0 upto 2^{2n-1} . The 2n-bit full precision product PFP can be written as

$$P_{FP} = X * Y = (x_{n-1}y_{n-1}2^{2n-2} + \sum_{i=0}^{n-2} \sum_{j=0}^{n-2} x_i y_j 2^{i+j} + 2^{n-1}(-2^{n-1} + \sum_{j=0}^{n-2} x_{n-1} y_j 2^j + D) + 2^{n-1}(-2^{n-1} + \sum_{i=0}^{n-2} y_{n-1} x_i 2^i + D)) \dots \dots \dots A$$

Equation 4 shows the Baugh Wooley algorithm [13]. The schematic circuit diagram of a 5-by-5 Baugh-Wooley array multiplier is shown in Figure 1.

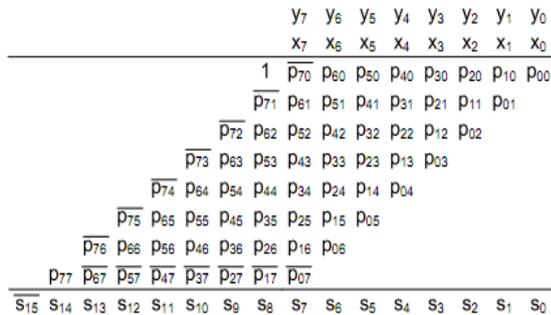
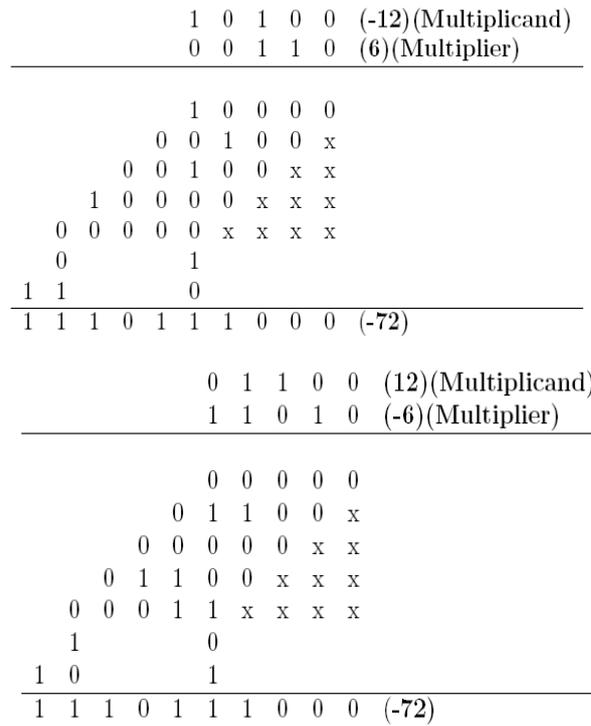
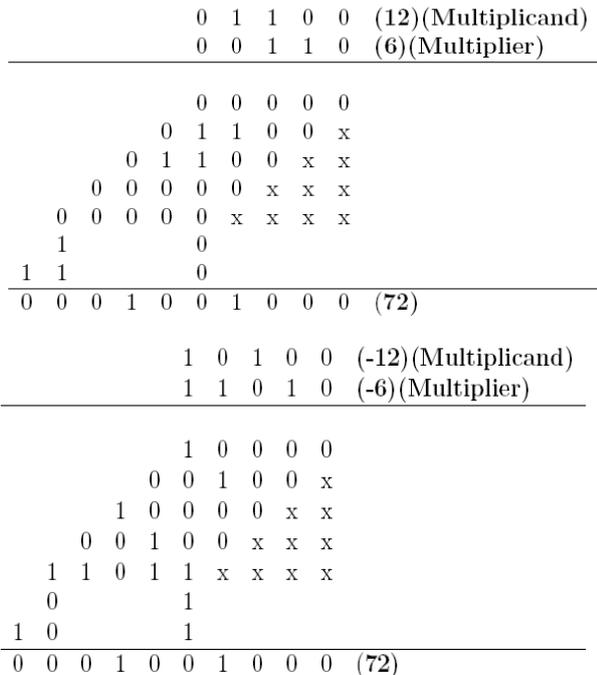


Figure 1: Schematic Circuit Diagram of a 5-by-5 Baugh-Wooley Array Multiplier

Example of Baugh-Wooley Algorithm



III. MODIFIED BAUGH WOOLEY MULTIPLIER

Conventional Baugh Wooley Multiplier method increases the height of the longest column by two, which may lead to a greater delay through the carry save adder tree. As shown in Tabular bit form 4.3, column height is 7, requiring an extra carry save adder level. Removing b4 from the fourth column and writing into b4 entries in the third column, which has only four entries, can reduce the extra delay. Thus, the maximum number of entries in one column becomes six. All negatively weighted a4b4 terms can be transferred to the bottom row, which leads to two negative numbers in the last two rows, where a subtraction operation from the sum of all the positive elements is necessary. Instead of subtracting a4b4 two's complement of a can be added b4 times. This method is known as the Modified Baugh Wooley Algorithm. Fig. 2 shows the schematic diagram of Modified Baugh Wooley algorithm for 5 X 5 bit multiplier.

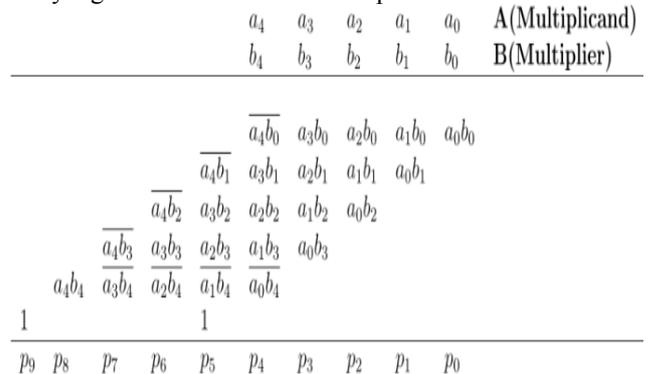


Figure 2: The Schematic Circuit Diagram of a 5-by-5 Modified Baugh-Wooley array multiplier.

IV. SIMULATION RESULTS AND DISCUSSION

The code for multiplier is written in Verilog language. The RTL Compiler is used to compile the code. The Encounter (cadence) software is used for floor planning, power

planning and routing purpose [22]. The functionality of the schematic is verified using Virtuoso (cadence) software. The major part of the design entry was done at the transistor schematic level. The layout where done in an attempt at estimating the area of the multiplier. Designs were entered using Cadence RTL compiler, using Encounter floor-planning, power-planning and routing is carried out. Cadence Virtuoso for pre layout and post layout simulation is using targeting NCSU AMI06 CMOS technology.

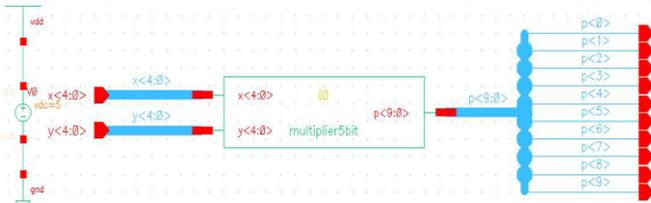


Figure 3: Test Bench Circuit for Simulation

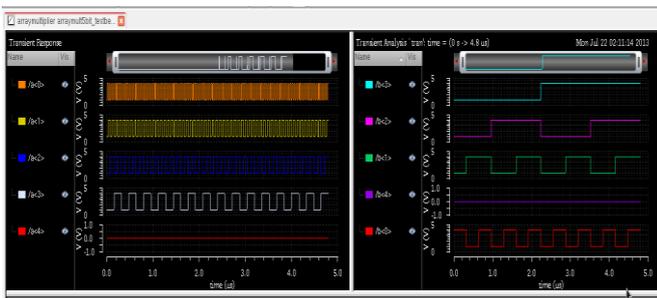


Figure 4: Functionality Proof: Two's Complement Array Multiplier Input Wave form

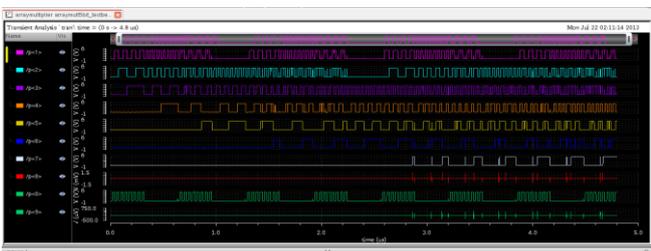


Figure 5: Functionality Proof: Two's Complement Array Multiplier Output Wave form

Figure 4 and Figure 5 show the input and output waveform of array multiplier. To verify the functionality of multiplier, the Analog Design Environment (ADL) is used.

When two numbers are negative, it will be in two's complement form. The two's complement of each is taken to convert it to a positive number, and then the two numbers are multiplied. The product is kept as a positive number and is given a sign bit of 0. Figure 6 and Figure 7 shows the input and output waveform of multiplication for two negative numbers. The resultant waveforms are compared with the test bench vectors written.

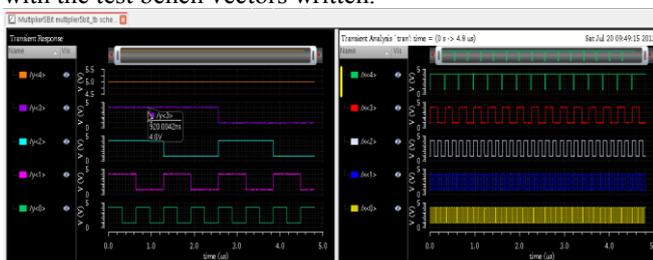


Figure 6: Functionality Proof: Baugh Wooley Multiplier Input Wave form: X- Negative Y- Negative

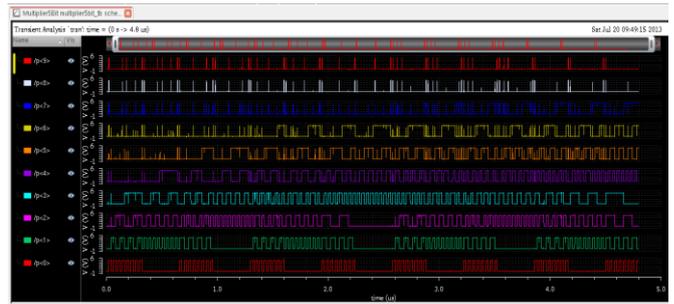


Figure 7: Output Waveform: X- Negative Y- Negative

TEST BENCH

The Test Bench is designed such that it can provide a series of stimuli to the Multiplier and vector (.vec) the results obtained. Simulation Result Files contains the multiplicand and multiplier sent to the Multiplier as well as the result received. In order to quickly validate the results, an automatic comparison is performed between the theoretical results and the experimental results. A block diagram of the Test Bench architecture is shown in Figure 8.

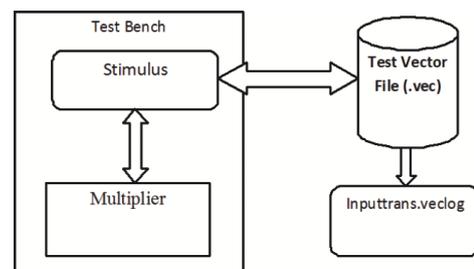


Figure 8: Test Bench Simulation Block Diagram

TEST VECTOR REPORT: The Test Bench is designed such that it can provide a series of stimuli to the Multiplier and vector (.vec) the results obtained. The Vector (.vec) file, included in Appendix B. Simulation Result Files contains the multiplicand and multiplier sent to the Multiplier as well as the result received. In order to quickly validate the results, an automatic comparison is performed between the theoretical results and the experimental results.

***VectorCheck for p < 0 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 175 Number of One's matched correctly = 64 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 1 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 143 Number of One's matched correctly = 96 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 2 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 127 Number of One's matched correctly = 112 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 3 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 119 Number of One's matched correctly = 120 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 4 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 107 Number of One's matched correctly = 132 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 5 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 99 Number of One's matched correctly = 140 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 6 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 79 Number of One's matched correctly = 160 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 7 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 46 Number of One's matched correctly = 193 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 8 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 14 Number of One's matched correctly = 225 Number of total states matched correctly = 239 Number of total errors = 0	
***VectorCheck for p < 9 >: All good! Number of total vector checks = 239 Number of X's matched correctly = 0 Number of Zero's matched correctly = 14 Number of One's matched correctly = 225 Number of total states matched correctly = 239 Number of total errors = 0	

Figure 9: Test vector report : Both Numbers are Negative

Delay Analysis (worst path)

Register transfer level (RTL) Timing Analysis (RTA) can provide accurate timing analysis of designs as early as possible in the design cycle. Performing timing analysis at the Register transfer level (RTL) level is faster and much more cost effective than waiting to find the same problems during timing analysis at the gate-level or layout-level. Figure 10 shows the worst case path for Modified Baugh Wooley Multiplier. If Slack time is positive, the tool is indicating that the signal arrives at the register on the right much earlier than is needed. This means that the circuit can work with a much higher clock frequency. As shown in figure 10, the path from input bit x[1] to output bit p[8] is having more delay compare to other. The total delay of worst case path is 6.219ns. The maximum clock frequency of the multiplier is 160MHz. If slack time becomes negative, then circuit does not meet timing. One has to find the maximum clock frequency upto which slack time is positive i.e. near to one. Table 5.6 shows the performance measures for various multiplier architectures. It is observed that the Modified Baugh Wooley multiplier is 1.5 times faster than Conventional Baugh Wooley multiplier.

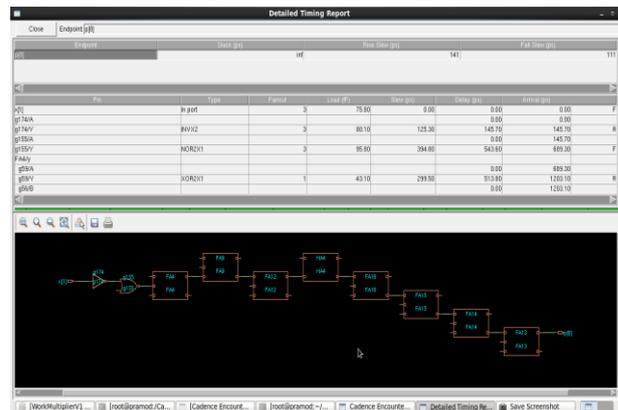


Figure 10: Timing Report: Worst Path Delay

Table 1: Comparison of various Multipliers

Multiplier Type	Power Dissipation (mW)	Area (μm^2)	Delay (ns)
Array Multiplier (Conventional)	8.909	83160	8.693
Baugh Wooley Multiplier	10.88	87912	9.62
Modified Baugh Wooley Multiplier	10.17	62646	6.219

Post Layout Simulation

The electrical performance of a full-custom design can be best analyzed by performing a post-layout simulation on the extracted circuit net-list. The detailed (transistor-level) simulation performed using the extracted netlist will provide a clear assessment of the circuit speed, the influence of circuit parasitic such as parasitic capacitances and resistances. After perform the LVS (Layout vs. Schematic), RC extraction of the design is carried out to find parasitic (resistance and capacitance) to carry out post layout simulations. Figure 11 shows the RC extracted diagram. Table 2 shows the power consumption of Modified Baugh Wooley Multiplier for the (Test Vector case: Both Numbers are positive) pre-layout and post-layout simulation. In Digital circuit, power consumption is increased in physical layout design due to parasitic components.



Figure 11: RC Extracted View of 5 Bit Modified Baugh Wooley Multiplier

Table 2: Comparison of Power Pre and Post Layout

	Pre layout (mW)	Post Layout (mW)
Modified Baugh Wooley Multiplier	7.36	7.47

V. CONCLUSION

An 5-bit signed multiplier was design using cadence IC615 using NCSU ami06, layout them in Encounter by cadence and the analysis of average dynamic power dissipation was done. The Modified Baugh wooley architecture is 109X faster than Conventional array multiplier and 102X faster than conventional Baugh Wooley. Baugh Wooley consumes more power as compared to conventional Baugh Wooley. Power can be further reduce by implementing the design using latest technological node such as 45nm, 65nm etc we can summarized some of the important design concepts as

1. Select the right structure before starting an elaborate circuit optimization.
2. Determine the critical timing path through the circuit.
3. Power and speed can be traded off through a choice of circuit sizing, supply voltage and transistor thresholds.

There is tremendous scope in design of multiplier in different architectures. The Baugh Wooley is used for 2's complement signed multiplication. There are other architectures for 2's complement signed multiplications. The same can be implemented using latest technology node such as 22nm, 32nm, 45nm which will reduce power and increase the speed.

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